the particular reciprocal lattice vector K used; the latter depends on the initial state k.

Figure 4-2 shows a cross section of the Brillouin zone for a b.c.c. lattice, taken in a 001 plane. The circles are cross sections of the Fermi surface and the dashed square is a zone for phonons, centered on the state k. The U.K. processes will be those for which the final state k' lies on that portion of the Fermi sphere centered at 0 which is outside the dashed square. A typical U.K. process and the associated phonon vector \vec{q} is shown. For fixed 0, the length $|\vec{q}|$ depends on the initial state \vec{k} ; this is most clearly seen by taking $0 = 180^{\circ}$ and \vec{k} first in the 100 and then in the 110 direction. For the latter direction $|\vec{q}|$ is about 1/4 as large as for k in the 100.

Normal processes must use longitudinal phonons, at least for those directions in which a separation into longitudinal and transverse modes is possible, because the term $\hat{e}_{q,p}^{\rightarrow}$. \hat{s} becomes $\hat{e}_{q,p}^{\rightarrow}$. \hat{q} for a normal process and this is zero for transverse modes. On the other hand, for an U.K. process \hat{s} is not usually parallel to \hat{q} and transverse phonons may participate; in fact the low value of the velocity of sound for transverse phonons will act as a weighting factor which emphasizes those U.K. processes which use transverse phonons.

One source of anisotropy in τ is then the k dependence of the contribution of $1/q^2$ to the integral for $\tau(\vec{k})$. This source occurs in any b.c.c. metal; for the case of the alkali metals the anisotropy of the velocity of sound must also be considered.

We now wish to make some estimate of the anisotropy of $\tau(\vec{k})$. The correct way to obtain $\tau(\vec{k})$ would be to choose a direction \vec{k} and compute q, $c^2_{\widehat{q},p}$, and $e_{\widehat{q},p}$ for a large number of points k' on a Fermi sphere and evaluate Eq. (IV-37). This would be a major computational task. A simpler but considerably less accurate procedure would be to consider only scattering in two dimensions and evaluate the θ integral in Eq. (IV-37) for fixed ϕ . Some of the loss of accuracy comes from the fact that for some k directions the θ integral depends strongly on the value of ϕ chosen. For example, if one chose k in the 110 direction and replaced the Brillouin zone for phonons

by a sphere of equal volume, there is ϕ symmetry in the sense that the $|\vec{q}|$ for fixed 0 is independent of ϕ , although $c_{\widehat{q},p}$ and $e_{\widehat{q},p}$. \widehat{s} are not; on the other hand, for k in a 111 direction this is not true. In a repeated zone scheme the nearest neighbor Fermi spheres do not have their centers on a 111 axis and consequently the section of these spheres cut by the plane containing k (111) and k' depends on ϕ . This makes it difficult to estimate $\tau(111)$ by doing only the 0 integration.

We decided to estimate the anisotropy in $\tau(\vec{k})$ by evaluating

$$I(\vec{k}) = \int_{0}^{2\pi} \frac{(1 - \cos \theta) |\sin \theta| [(JS)\theta]^{2} d\theta}{|\vec{q}|^{2}}$$
(IV-40)

for \vec{k} in the 100, 110, and 111 directions. This is a very crude procedure, which not only replaces the three dimensional integration in Eq. (IV-37) by a two dimensional one, but also considers the velocity of sound, the polarization factor $\hat{e}_{\hat{q},p}$. \hat{s} , and the density of states as constants. Although we could have approximated $c_{\hat{q},p}^2$ in Eq. (IV-37) by using the velocity of sound in the principal direction closest to that of \vec{q} , we felt this procedure ran the risk of weighting the integral by the sound velocity for an unrepresentative phonon; it would also give a factor $\frac{1}{c_{\hat{q},p}^2}$ that was discontinuous in 0.

We obtained the values of $(JS)^2$ given by Bailyn [13]; in Table IV-4 we list his values of $u^3(JS)^2$ vs. $u = \frac{\sin \theta}{2}$ for potassium and lithium. The square of the matrix element for potassium has values less than those for rubidium and cesium and greater than those for sodium; the general behavior of $(JS)^2$ vs. u is similar for all these four metals and we chose potassium as representative of them. Lithium is unlike the other alkalis in that $(JS)^2$ goes through a zero near $\theta = 120^{\circ}$. In Fig. 4-3 we have plotted

$$F(\theta) = (JS)^2 (1 - \cos \theta) \sin \theta$$
 (IV-41)

for 9 from 0 to 180° in a polar plot, using Bailyn's values for the potassium and lithium matrix elements. For 9 from 180° to 360° the absolute value of sin 9 should be used. F(9) peaks rather sharply near 75° for lithium; this